

Performance Evaluation of FPM on Spartan Family FPGAs and Analyze Its Effect on Bonded IOBs

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Abstract — VHDL programming for IEEE single precision floating point multiplier module have been explored because floating point multiplication is a most widely used operation in DSP/Math processors, robots, air traffic controller, digital computers. Because of its vast areas of application, the main emphasis is on the implementing it effectively such that it uses less combinational delay with high Speed. Floating point operations are hard to implement on FPGAs i.e. on reconfigurable hardware's because of their complexity of their algorithms. On the other hand, many scientific problems require floating point arithmetic with high level of accuracy in their calculations. The parameter number of bonded IOBs (Input Output Blocks) has been analyzed while implementing the floating point multiplier on Spartan 2, Spartan 2E, Spartan 3 and Spartan 3E FPGA's.

Keywords - Floating Point Multiplier, FPGAs, Memory, Xilinx and Spartan.

I. INTRODUCTION

Many people consider floating-point arithmetic an esoteric subject. This is rather surprising because floating-point is ubiquitous in computer systems. Almost every language has a floating-point data type. Floating Point numbers represented in IEEE 754 format are used in most of the DSP Processors. Floating point arithmetic is useful in applications where a large dynamic range is required or in rapid prototyping applications where the required number range has not been thoroughly investigated. The floating Point Multiplier IP helps designers to perform floating point Multiplication on FPGA represented in IEEE 754 single precision floating point format. The single precision multiplier is divided into three main parts corresponding to the three parts of the single precision format [1]. The normalized floating point numbers have the form of

$$Z = (-1)^s * 2^{(E - Bias)} * (1.M) \quad (1)$$

Where $M = m_{22} 2^{-1} + m_{21} 2^{-2} + m_{20} 2^{-3} + \dots + m_1 2^{-22} + m_0 2^{-23}$;

Bias = 127.

The first part of the floating point multiplier is sign which is determined by an exclusive OR function of the two input signs. The second part is the exponent which is calculated by adding the two input exponents. The third part is significand or mantissa which is determined by multiplying the two input significands each with a "1" concatenated to it. That "1" is the hidden bit. The main applications of floating points today are in the field of medical imaging, biometrics, motion capture and audio

applications, including broadcast, conferencing, musical instruments and professional audio.

II. FPGA

(FIELD PROGRAMMABLE GATE ARRAY)

FPGA stands for Field Programmable Gate Array. It is a semiconductor device containing programmable logic components and programmable interconnects. The programmable logic components can be programmed to duplicate the functionality of basic logic gates such as AND, OR, XOR, NOT or more complex combinational functions such as decoders or simple mathematical functions [3] [8].

In most FPGAs, these programmable logic components (or logic blocks, in FPGA parlance) also include memory elements, which may be simple flip flops or more complete blocks of memories. A hierarchy of programmable interconnects allows the logic blocks of an FPGA to be interconnected as needed by the system designer, somewhat like a one-chip programmable breadboard shows in figure 1. These logic blocks and interconnects can be programmed after the manufacturing process by the customer/designer (hence the term "field programmable", i.e. programmable in the field) so that the FPGA can perform whatever logical function is needed [4].

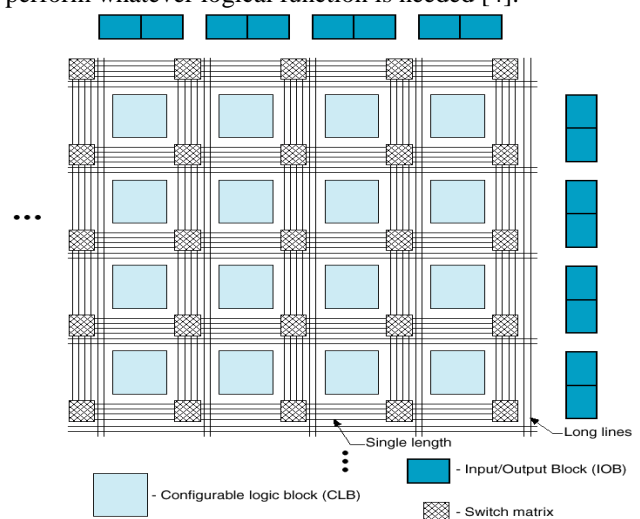


Fig.1. FPGA board

FPGAs are generally slower than their application specific integrated circuit (ASIC) counterparts, as they can't handle as complex a design, and draw more power. However, they have several advantages such as a shorter

time to market, ability to re-program in the field to fix bugs, and lower non recurring engineering cost costs. Vendors can sell cheaper, less flexible versions of their FPGAs which cannot be modified after the design is committed. The development of these designs is made on regular FPGAs and then migrated into a fixed version that more resembles an ASIC. Complex programmable logic devices, or CPLDs, are another alternative.

III. FLOATING POINT FORMAT

The advantage of floating point format over fixed point format is the range of numbers that can be presented with the fixed number of bits. Floating point number is composed of three fields and can be of 16, 18, 32 and 64 bit. Figure shows the IEEE standard for floating point numbers [2].

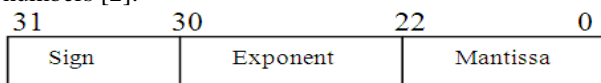


Fig.2. Standard for floating point numbers

1 bit sign of signifies whether the number is positive or negative. '1' indicates negative number and '0' indicate positive number. 8 bit exponent provides the exponent range from E (min) =-126 to E (max) =127. 23 bit mantissa signifies the fractional part of a number the mantissa must not be confused with the significand. The leading '1' in the significant is made implicit [3].

A. Conversion of Decimal to Floating numbers

Conversion of Decimal to Floating point 32 bit formats is explained in 1 & 2 example.

Example:

Step 1: Suppose a decimal number 129.85 is taken.

Step 2: Convert it into binary number of 24 bits

i.e.10000001.1101110000000000.

Step 3: Shift the radix point to the left such that there will be only one bit which is left of the radix point and this bit must be 1. This bit is known as hidden bit.

Step 4: Count the number of times radix points is shifted to the left say 'x'. The number which is formed after shifting of radix point is 1.00000011101110000000000. Here x=7.

Step 5: The number which is after the radix point is called mantissa which is of 23 bits and the whole number including hidden bit is called significand which is of 24 bits.

Step 6: The value 'x' must be added to 127 to get the original exponent value which is 127 + 'x'. In this case exponent is 127 + 7 = 134 which is 10000110.

Step 7: Number is +ve hence MSB of number is 0.

Step 8: Now assemble result into 32 bit format in the form of sign, exponent and mantissa

01000011000000011101110000000000.

IV. MULTIPLICATION ALGORITHM FOR FLOATING POINT NUMBERS

As stated in the introduction, normalized floating point numbers have the form of

$$Z = (-1)^s * 2^{(E - Bias)} * (1.M) \quad (1)$$

Where $M = m_{22} 2^{-1} + m_{21} 2^{-2} + m_{20} 2^{-3} + \dots + m_1 2^{-22} + m_0 2^{-23}$;

Bias = 127.

To multiply two floating point numbers the following steps are taken [1] [6]:

Step 1: Multiplying the significand; i.e. (1.M1*1.M2)

Step 2: Placing the decimal point in the result

Step 3: Adding the exponents; i.e. (E1 + E2 - Bias)

Step 4: Obtaining the sign; i.e. s1 xor s2 and put the result together

Step 5: Normalizing the result; i.e. obtaining 1 at the MSB of the results' significand shown in figure 3.

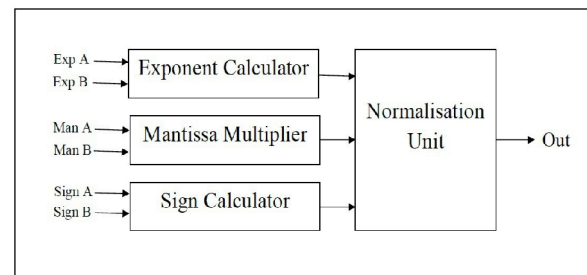


Fig.3. Normalization of sign, exponent and mantissa

We present a floating point multiplier in which rounding technique is implemented. Rounding support can be added as a separate unit that can be accessed by the multiplier or by a floating point adder, thus accommodating for more precision. The multiplier structure; Exponents addition, Significand multiplication, and Result's sign calculation are independent shown in figure 5.4. The significand multiplication is done on two 24 bit numbers and results in a 48 bit product, which we will call the intermediate product (IP). The IP is represented as (47 downto 0). The following sections detail each block of the floating point multiplier.

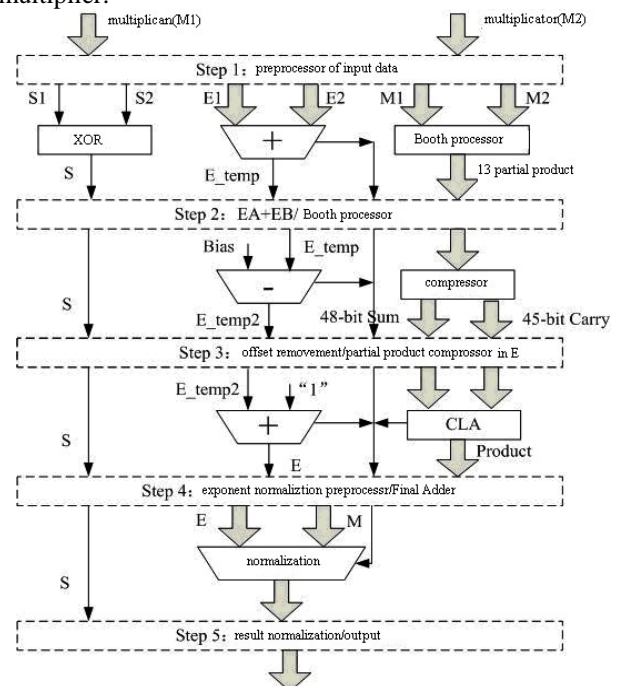


Fig.4. Algorithm for floating point multiplication

B. An example of floating point multiplier with proposed algorithm

A: 0 1000111 10010101001110000101000 (32 bit)
 B: 0 1000110 10010010011010111000010 (32 bit)
 To multiply A and B
 Step 1: Multiplying the significand (including hidden bit)
 110010101001110000101000 (24 bit)*
 110010010011010111000010 (24 bit)
 =100111100111110010011101000110100111100101000 (48 bit)
 Step 2: Placing the decimal point in the result
 10.0111110011111100100111010001101001111001010000
 Step 3: Adding the exponents; i.e. (E1 + E2 - Bias)
 Adding of exponents =10000111 (E1) +10000110 (E2)
 The exponent representing the two numbers is already shifted/biased by the bias value (127) and is not the true exponent; i.e. EA = EA-true + bias and EB = EB-true + bias And EA + EB = EA-true + EB-true + 2 bias
 So we should subtract the bias from the resultant exponent otherwise the bias will be added twice.
 Exponent Result = 10000111 (E1) +10000110 (E2) - 01111111 (Bias 127) = 10001110
 Eresult = 10001110
 Step 4: Obtaining the sign; i.e. s1 xor s2 and put the result together
 0 Xor 0 = 0, so the sign of the number is +ve
 0 10001110
 10.0111110011111100100111010001101001111001010000
 Step 5: Normalizing the result
 Normalize the result so that there is a 1 just before the radix point (decimal point). Moving the radix point one place to the left increments the exponent by 1; moving one place to the right decrements the exponent by 1
 Before Normalizing
 0 10001110
 10.0111110011111100100111010001101001111001010000
 After normalization
 0 10001111
 1.0011110011111100100111010001101001111001010000 (including hidden bit)
 Step 6: Rounding the result to the nearest number [3] [5]
 The mantissa bits are more than 23 bits (mantissa available bits); rounding is needed. If we applied the round to nearest rounding mode then the stored value is:
 01000111001111001111100100111(After rounding)
 Step 7: Checking for underflow/overflow occurrence
 There are four main cases that the exponent is affected by normalization. It depends upon the Eresult that is calculated above [7] i.e.

Table 1 Normalization effect on result's Exponent and Overflow/Underflow detection

Eresult	Category	Comments
-125 Eresult < 0	Underflow	Can't be compensated during normalization

Eresult = 0	Zero	May turn to normalized number during normalization (by adding 1 to it)
1 < Eresult < 254	Normalized number	May result in overflow during Normalization
255 Eresult	Overflow	Can't be compensated

There are some special conditions while implementing floating point multiplier which needs to be handle these are explained in table.

The flow graph of overall algorithm for floating point multiplier including rounding is shown in figure 5.

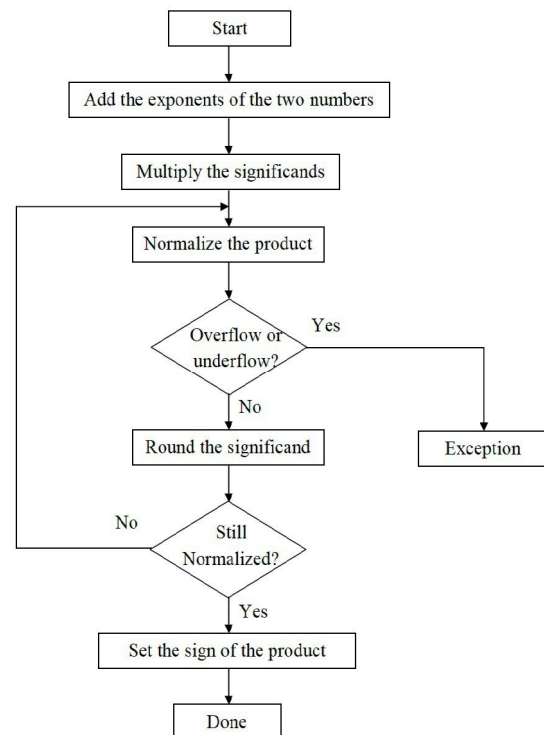


Fig.5. Floating point multiplier flow graph

V. FINAL RESULTS/SYNTHESIS REPORT

Results of Spartan 2, Spartan 2e, Spartan 3 and Spartan 3e, FPGA modules with different devices and speed grades are shown in table.

Table 2 Results/ Synthesis report

S. No.	FPGA's	Speed Grade	Number of Bonded IOBs	Utilization in %age
1.	Spartan2 (XC2S100-TQ144)	-6	96/96	100
2.	Spartan2E (XC2S50E-FT256)	-7	96/182	52
3.	Spartan3 (XC3S50-PQ208)	-5	96/124	77
4.	Spartan3E (XC3S250E-TQ144)	-5	96/108	88

VI. SIMULATION WAVEFORM (USING MODEL SIM SIMULATOR)

Case 1: When both the numbers are of same sign

1st input no. 405.22 =
01000011110010101001110000101000
2nd input no. 201.21 =
01000011010010010011010111000010
Desired output no. 81534.31 =
01000111100111110011111100100111

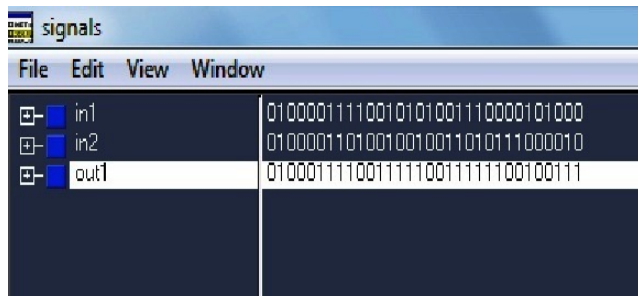


Fig.6. Signals in Model Sim

Simulation result 81534.31 =
01000111100111110011111100100111

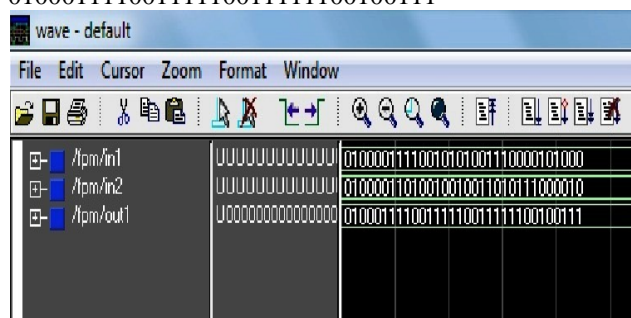


Fig.7. Simulation result for Floating point multiplier

Case 2: When both the numbers are of different sign

1st input No. 721.51 =
01000100001101000110000010100011
2nd input No -902.12 =
11000100011000011000011110101110
Desired output no -650888.6 =
11001001000111101110100010001000

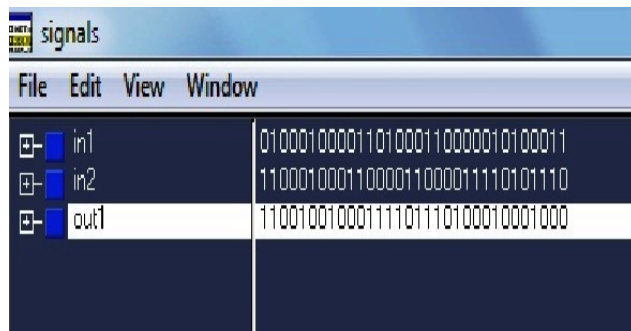


Fig.8. Signals in Model Sim

Simulation result -650888.6 =
11001001000111101110100010001000

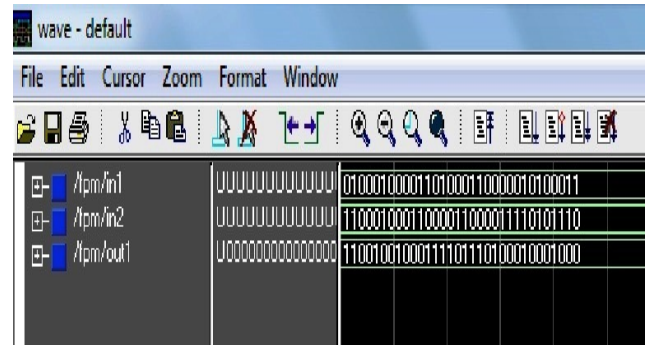


Fig.9. Simulation result for Floating point multiplier

VII. CONCLUSIONS

The floating point multiplier has been designed, optimized and implemented on Spartan 2, Spartan 2E, Spartan 3, and Spartan 3E FPGA modules. From the final results it is concluded that implementation of floating point multiplier on Spartan2E (XC2S50E-FT256) with speed grade -7 causes small bonded IOBs i.e. 96/182 (52%).

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